

Key

1. Use slope-intercept form to find the equation of the line having a slope of 3 and a y-intercept of 5.

$$y = mx + b$$

$$y = 3x + 5$$

2. Determine the equation of a line passing through the point (5, -3) with an undefined slope.

Vertical line $x = 5$

3. Determine the equation of a line passing through the point (-4, 2) with a slope of 0.

Horiz. line $y = 2$

4. Use point-slope form to find the equation of the line passing through the point (0, 5) with a slope of 2/3.

$$y - y_1 = m(x - x_1)$$

$$y - 5 = \frac{2}{3}(x - 0)$$

$$y - 5 = \frac{2}{3}x$$

5. Find the equation of a line passing through the point (2, 8) and parallel to the line $y = \frac{5}{6}x - 1$.

$$y - 8 = \frac{5}{6}(x - 2) \quad \text{point slope}$$

$$m = \frac{5}{6}$$

$$6y - 48 = 5x - 10$$

$$5x - 6y = -38 \quad \text{standard form}$$

$$y = \frac{5}{6}x + \frac{38}{6} \quad \text{slope-intercept form}$$

6. Find the equation of a line perpendicular to the y-axis passing through the point (4, 7).

$$\begin{array}{l} y - \text{axis } m = \text{und} \\ \perp m = 0 \end{array} \quad y - 7 = 0(x - 4)$$

$$y = 7$$

7. Find the equation of a line passing through the points (-3, 6) and (1, 2).

$$m = \frac{2-6}{1-(-3)} = \frac{-4}{4} = -1$$

$$y - 6 = -1(x - (-3))$$

$$y - 6 = -x - 3$$

$$y = -x + 3$$

8. Find the equation of a line with an x-intercept (2, 0) and a y-intercept (0, 3).

$$m = -\frac{3}{2} \quad y = -\frac{3}{2}x + 3$$

Using the point-slope form $y - y_1 = m(x - x_1)$, write an equation for the line

1. with slope -2, containing the point (3, 4) 1. $y - 4 = -2(x - 3)$

2. containing the points (1, -3) and (-5, 2)

$$m = \frac{2-(-3)}{-5-1} = \frac{5}{-6}$$

$$2. \quad y - 2 = -\frac{5}{6}(x + 5) \quad \text{or} \quad y + 3 = -\frac{5}{6}(x - 1)$$

3. with slope 0, containing the point (4, 2)

$$3. \quad y = 2$$

4. perpendicular to the line in problem #1, containing the point (3, 4)

$$m = \frac{1}{2}$$

$$4. \quad y - 4 = \frac{1}{2}(x - 3)$$

(1)

I. Polynomials

A. Factor Completely.

$$1) t^2 - 4t - 21 \\ (t - 7)(t + 3)$$

$$2) x^3 - 8 \\ (x - 2)(x^2 + 2x + 4)$$

$$3) 27x^3 + 125 \\ (3x + 5)(9x^2 - 15x + 25)$$

$$4) 10m^5n^2 - 15m^2n + 25m \\ 5m(2m^3n^2 - 3mn + 5)$$

$$5) 25x^2 - 49 \\ (5x + 7)(5x - 7)$$

$$6) x^3 - 2x^2 - 4x + 8 \\ x^2(x - 2) - 4(x - 2) \\ (x^2 - 4)(x - 2) \\ (x + 2)(x - 2)(x - 2)$$

B. Simplify the following expressions.

$$1) (-3x^2 + 4x - 7) + (2x^2 - 7x + 8) \\ -x^2 - 3x + 1$$

$$2) 5x^2 \cdot 2x^5 \\ 10x^7$$

$$3) (-2c^3)^2 \\ 4c^6$$

$$4) (39a^4 - 4a^3 + 2a^2 - a - 7) - (10a^4 + 3a^3 - 2a^2 - a + 8) \\ 29a^4 - 7a^3 + 9a^2 - 15$$

$$5) \frac{283x^{-5}y^{21}}{6x^{-5}y^{25}} = \frac{283x^{10}}{6y^4}$$

$$6) (3x + 7)(2x + 5) \\ 6x^2 + 29x + 35$$

$$7) -3xy^3(x - 2y) \\ -3x^2y^3 + 6xy^4$$

$$8) (3x^2 + x - 1)(2x - 3) \\ 6x^3 - 9x^2 + 2x^2 - 3x - 2x + 3 \\ 6x^3 - 7x^2 - 5x + 3$$

$$9) (8a^3b^2)(2ab) \\ 16a^4b^3$$

$$10) (-3x^2y^3z)^3 \\ -27x^6y^9z^3$$

$$11) (15a^4b^2c)^0 \\ 1$$

$$12) \frac{3x^3y^2}{6x^2y^5} \cdot \frac{x}{2y^3}$$

$$13) (x + 6)^2 \\ x^2 + 12x + 36$$

$$14) t^3 \cdot t^{(n-3)} \\ t^3 (t^n \cdot t^{-3}) \\ t^n \cdot t^0 = t^n$$

$$15) (x^m)^n \cdot (x^n)^{n-m} \\ x^{mn} \cdot x^{n^2} \cdot x^{-nm} \\ x^{n^2} \cdot x^0 = x^{n^2}$$

$$16) \frac{4^{h-k}}{4^{h-k}} = \frac{4^h \cdot 4^{-k}}{4^h \cdot 4^k} = \frac{1}{4^{2k}}$$

C. Solve the following quadratic equations for x.

$$1) (2x+1)(x+3) = 0 \\ 2x+1=0 \quad x+3=0 \\ x = -\frac{1}{2} \quad x = -3$$

$$2) x^2 + 6x = 0 \\ x(x+6) = 0 \\ x = 0 \quad x = -6$$

$$3) 2x^2 + 4x = -3 \\ 2x^2 + 4x + 3 = 0 \text{ does not factor} \\ -4 \pm \sqrt{16 - 4(2)(3)} = \frac{-4 \pm \sqrt{-8}}{4}$$

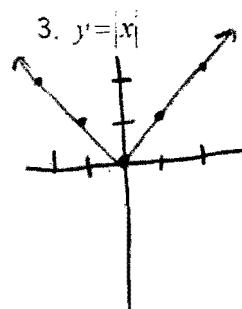
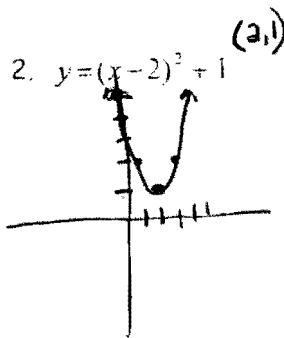
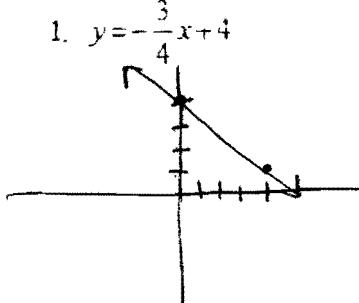
$$4) x^2 = 16 \\ x = \pm \sqrt{16} \\ x = \pm 4$$

$$= \frac{-4 \pm 2i\sqrt{2}}{4} = \frac{-2 \pm i\sqrt{2}}{2}$$

(2)

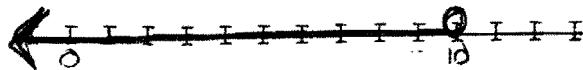
II. Linear Operations/Solving Inequalities

A. Create your own grid and graph the following equations.

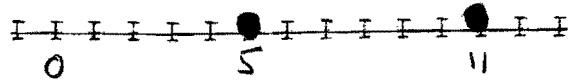


B. Solve the inequality and graph the solution set on a number line:

$$\begin{aligned} 1. \quad & 4(t+2) - 3 > 7(t+5) \\ & 4t + 8 - 3 > 7t + 35 \\ & -3t > 30 \\ & t < -10 \end{aligned}$$



$$\begin{aligned} 2. \quad & |x - 8| = 3 \\ & x - 8 = 3 \quad x - 8 = -3 \\ & x = 11 \quad x = 5 \end{aligned}$$



C. Answer each of the following concerning linear equations.

If question does not specify, leave answers in any acceptable equation of a line

1) Determine the slope of the line containing the points $(6, -2)$ and $(-1, 5)$.

$$m = \frac{5 - (-2)}{-1 - 6} = \frac{7}{-7} = -1$$

2) Determine an equation for a line with slope $\frac{1}{2}$ and y-intercept at $(0, -3)$.

$$y = \frac{1}{2}x - 3$$

3) Determine an equation for a line parallel to $y = -3x + 4$ containing the point $(2, 1)$.

$$m = -3 \quad y - 1 = -3(x - 2)$$

4) Line m is perpendicular to $y = 4x - 1$ and passes through the origin. What is the equation of line m .

$$m = -\frac{1}{4} \quad (0, 0) \quad y - 0 = -\frac{1}{4}x$$

$$y = -\frac{1}{4}x$$

③

$$1. \frac{\sqrt{x}}{x} \frac{x^6}{X} = \frac{1}{x^{1/2}}$$

$$2. e^{\ln 3}$$

$$3$$

$$3. e^{(1+\ln x)} e^1 \cdot e^{\ln x} = ex$$

$$4. \ln 1$$

$$0$$

$$5. \ln e^7$$

$$7$$

$$6. \log_3(1/3) = x$$

$$\begin{aligned} 3^x &= \frac{1}{3} \\ 3^x &= 3^{-1} \\ x &= -1 \end{aligned}$$

$$7. \log_{1/2} 8 = x$$

$$\begin{aligned} \frac{1}{2}^x &= 8 \\ \frac{1}{2}^x &= 2^3 \\ 2^{-x} &= 2^3 \\ x &= -3 \end{aligned}$$

$$8. \ln \frac{1}{2} \text{ use calculator}$$

$$- .693$$

$$9. \frac{e^{3\ln x}}{e^{\ln x^3}}$$

$$X^3$$

$$10. \frac{4xy^{-2}}{12x^{-1/3}y^{-5}}$$

$$\frac{1}{3} x^{4/3} y^3$$

$$11. 27^{2/3}$$

$$9$$

$$\sqrt[3]{27}^2$$

$$12. (5a^{2/3})(4a^{3/2})$$

$$20 a^{13/6}$$

$$13. (4a^{5/3})^{3/2}$$

$$\frac{8a^{15/6}}{\sqrt{4^3}} = 8a^{5/2}$$

$$14. \frac{3(n+1)!}{5n!}$$

$$\frac{3(n+1)!}{5n!}$$

$$\text{Simplify}$$

$$1. 5\log x + 7\log y = \log_3 x^5 y^7$$

$$14. \frac{3(n+1)!}{5n!}$$

$$\text{Solve}$$

$$2. 6\log x - 4\log y - 2\log z = \log \frac{x^6}{y^4 z^2}$$

$$\ln 3^x = \ln 8$$

$$3. 3(\log x - 4\log y) = 3(\log \frac{x}{y^4}) = \log_3 \frac{x^3}{y^{12}}$$

$$x \ln 3 = \ln 8$$

$$4. \frac{\log x + 4\log y}{x} + \log x^4 = \log x^4 = \log \frac{1}{x^4}$$

$$x = \frac{\ln 8}{\ln 3} = 1.893$$

$$5. 20\log \sqrt{x} = \log(x^{1/5})^20 = \log x^4$$

$$5^x = 12$$

$$6. 3\log x - \log \frac{1}{y} = \log_3 \frac{x^3}{y} = \log_3 x^3 y$$

$$5^x = 12/5$$

$$7. \frac{1}{2}(\log x + 3\log y) - 2\log z$$

$$x \ln 5 = \ln 12/5$$

$$\frac{1}{2}(\log x + \log y^3) - \log z^2$$

$$x = \frac{\ln 12/5}{\ln 5} = 0.84$$

$$\frac{1}{2}\log x y^3 - \log z^2 = \log \frac{x^{1/2} y^{3/2}}{z^2}$$

$$5^x = 3$$

$$(\frac{5}{3})^x = 3$$

$$x \ln \frac{5}{3} = \ln 3$$

$$x = \frac{\ln 3}{\ln 5/3} = 0.594$$

$$x = \frac{\ln 3}{\ln$$

Key



Solving Quadratic Equations Assignment

1. Solve for x.

a. $x^2 + 7x - 18 = 0$
 $(x + 9)(x - 2) = 0$
 $x = -9, 2$

b. $x^2 + x + \frac{1}{4} = 0$
 $(2x^2 + 4x + 1) = 0$
 $2x^2 + 4x + 1 = 0$
 $x = -\frac{1}{2}$

c. $2x^2 - 72 = 0$
 $2(x^2 - 36) = 0$
 $2(x+6)(x-6) = 0$
 $x = -6, 6$

d. $12x^2 - 5x = 2$
 $12x^2 - 5x - 2 = 0$
 $(3x - 2)(4x + 1) = 0$
 $x = 2/3, -1/4$

e. $20x^2 - 56x + 15 = 0$
 $(5x - 3)(4x - 5) = 0$
 $x = 3/10, 5/4$

f. $81x^2 + 72x + 16 = 0$
 $(9x+4)(9x+4) = 0$
 $x = -4/9$

g. $x^2 + 10x = 7$
 $x^2 + 10x - 7 = 0$
 $x = \frac{-10 \pm \sqrt{10^2 - 4(1)(-7)}}{2}$
 $x = \frac{-10 \pm \sqrt{108}}{2} = \frac{-10 \pm 8\sqrt{3}}{2}$
 $x = -5 \pm 4\sqrt{3}$

h. $3x - 4x^2 = -5$
 $-4x^2 + 3x + 5 = 0$
 $x = \frac{3 \pm \sqrt{9 - 4(-4)(5)}}{-8}$
 $x = \frac{3 \pm \sqrt{89}}{-8}$

i. $7x^2 - 7x + 2 = 0$
 $x = \frac{7 \pm \sqrt{49 - 4(7)(2)}}{14} = \frac{7 \pm \sqrt{17}}{14}$
 $x = \frac{7 \pm i\sqrt{17}}{14}$ or $\frac{1}{2} \pm \frac{i\sqrt{17}}{14}$

j. $x + \frac{1}{x} = \frac{17}{4}$
 $x^2 + 1 = \frac{17}{4}x$
 $x^2 - \frac{17}{4}x + 1 = 0$
 $4x^2 - 17x + 4 = 0$
 $x = \frac{17 \pm \sqrt{289 - 4(4)(4)}}{8} = \frac{17 \pm 15}{8}$
 $x = 4, \frac{1}{4}$

k. $x^3 - 5x^2 + 5x - 25 = 0$
 $x^2(x-5) + 5(x-5) = 0$
 $(x-5)(x^2 + 5) = 0$
 $x = 5, \pm i\sqrt{5}$

l. $2x^4 - 15x^3 + 18x^2 = 0$
 $x^2(2x^2 - 15x + 18) = 0$
 $x^2(2x-3)(x-6) = 0$
 $x = 0, 3/2, 6$

② If $y = x^2 + kx - k$, for what values of k will the quadratic have two real solutions?

$$K = -4$$

3. Find the domain of $y = \frac{2x-1}{6x^2-5x-6}$

$$6x^2 - 5x - 6 = 0$$

$$(3x+2)(2x-3) = 0$$

$$x \neq -\frac{2}{3}, \frac{3}{2}$$

(5)

*tricky!

Special Factorization - Assignment

- Completely factor the following expressions

$$1. \quad x^3 - 25x \\ x(x^2 - 25) \\ x(x+5)(x-5)$$

$$2. \quad 30x - 9x^2 - 25 \\ -9x^2 + 30x - 25 \\ -(9x^2 - 30x + 25) \\ -(3x-5)(3x-5)$$

$$3. \quad 3x^2 - 5x^2 + 2x \\ -2x^2 + 2x \\ -2x(x-1)$$

$$4. \quad 3x^8 - 3 \\ 3(x^8 - 1) \\ 3(x-1)(x^2 + x + 1)$$

$$5. \quad 16x^4 - 24x^3y + 9y^2 \\ (4x^2 - 3y)(4x^2 - 3y)$$

$$6. \quad 9a^4 - a^2b^2 \\ a^2(9a^2 - b^2) \\ a^2(3a+b)(3a-b)$$

$$7. \quad 4x^4 + 7x^2 - 36 \\ (4x^2 - 9)(x^2 + 4) \\ (2x+3)(2x-3)(x^2 + 4)$$

$$8. \quad 250x^3 - 128 \\ 2(125x^3 - 64) \\ 2(5x-4)(25x^2 + 20x + 16)$$

$$9. \quad \frac{8x^3}{125} + \frac{64}{y^3} = 8\left(\frac{x}{5}\right)^3 + \left(\frac{4}{y}\right)^3 \\ 8\left(\frac{x}{5} + \frac{4}{y}\right)\left(\frac{x^2}{25} - \frac{2x}{5y} + \frac{16}{y^2}\right)$$

$$10. \quad x^5 + 17x^3 + 16x \\ x(x^4 + 17x^2 + 16) \\ x(x^2 + 16)(x^2 + 1)$$

$$11. \quad 144 + 32x^2 - x^4 \\ -x^4 + 32x^2 + 144 \\ -(x^4 - 32x^2 - 144) \\ -(x^2 + 36)(x^2 + 4)$$

$$12. \quad 16x^{2a} - y^{8a} \\ (4x^{2a} + y^{4a})(4x^{2a} - y^{4a}) \\ (4x^{2a} + y^{4a})(2x^a + y^4)(2x^a - y^4)$$

$$13. \quad x^3 - xy^2 + x^2y - y^3 \\ x(x^2 - y^2) + y(x^2 - y^2) \\ (x-y)(x+y)(x+y) \\ (x+y)^2(x-y)$$

$$14. \quad x^6 - 9x^4 - 81x^2 + 729 \\ x^4(x^2 - 9) - 81(x^2 - 9) \\ (x^2 - 9)(x^4 - 81) \\ (x+3)(x-3)(x^2 + 9)(x^2 - 9) \\ (x+3)(x-3)(x+9)(x+3)(x-3)$$

$$15. \quad x^2 - 8xy + 16y^2 - 25 \\ (x-4y)(x-4y) - 25 \\ (x-4y)^2 - 25 \\ [(x-4y) + 5]\sqrt{(x-4y) - 5}$$

$$16. \quad x^5 + x^3 + x^2 + 1 \\ x^3(x^2 + 1) + (x^2 + 1) \\ (x^2 + 1)(x^3 + 1) \\ (x^2 + 1)(x+1)(x^2 - x + 1)$$

$$17. \quad x^6 - 1 \\ (x^3 - 1)(x^3 + 1) \\ (x-1)(x^2 + x + 1)(x+1)(x^2 - x + 1)$$

$$18. \quad x^6 + 1 \quad (x^2)^3 + (1)^3 \\ (x^2 + 1)(x^4 - x^2 + 1)$$

(6)

Given $f(x) = 7 - x^2$ and $g(x) = x - 4$, find each value.

1. $f(-4)$

$$7 - 16 = -9$$

2. $g(-4)$

$$-8$$

3. $f(g(-2))$

$$f(-6) = 7 - 36 = -29$$

4. $f(4a)$

$$7 - (4a)^2 = \\ 7 - 16a^2$$

5. $f(t+1)$

$$7 - (t+1)^2 = 7 - (t^2 + 2t + 1) \\ 7 - t^2 - 2t - 1 = \\ -t^2 - 2t + 6$$

6. $[f \circ g](x) = f(g(x))$

$$7 - (x^2 - 8x + 16) = -x^2 + 8x - 9$$

7. $[g \circ f](x) = g(f(x))$

$$7 - x^2 - 4 = -x^2 + 3$$

Given the following functions, $f(x) = -3(x-2)^2 - 1$ and $g(x) = \frac{2x-3}{x+5}$, find:

8. a. $f(g(2))$

$$g(2) = \frac{1}{7}$$

b. $g(f(2))$

$$f(2) = -1$$

$$f\left(\frac{1}{7}\right) = -3\left(-\frac{13}{7}\right)^2$$

$$= -3\left(\frac{169}{49}\right) = \frac{-507}{49} = \frac{49}{49}$$

$$g(-1) = \boxed{\frac{-5}{4}}$$

$$\boxed{-\frac{556}{49}}$$

9. If $g(x) = x^2 - 5x + 12$ then find:

a. $g(-6) 36 + 30 + 12 = \boxed{78}$

b. $g(x-2)$

$$\begin{aligned} & (x-2)^2 - 5(x-2) + 12 \\ & x^2 - 4x + 4 - 5x + 10 + 12 \\ & \boxed{x^2 - 9x + 26} \end{aligned}$$

Simplify the following rational expressions.

10.

$$\frac{\frac{x}{4} + \frac{2x}{3}}{\frac{3x}{12} + \frac{8x}{12}} = \boxed{\frac{11x}{12}}$$

11.

$$\frac{7x^2}{8} \cdot \frac{14}{9x} = \boxed{\frac{7x}{12}}$$

12.

$$\frac{2}{3} \div \frac{1}{4} = \boxed{\frac{8}{3}}$$

$$(x-5)(x+4)$$

13.

$$\frac{x^2 - x - 20}{x+4} \cdot \frac{x-3}{x^2 - 2x - 15}$$

$$\boxed{\frac{x-3}{x+3}}$$

$$(x-5)(x+3)$$

Solve the equation:

$$-2x - 2 = x + 3$$

$$-3x = 5$$

$$\boxed{x = -5/3}$$

14.

$$\frac{2x+1}{x^2-4} + \frac{5}{x-2}$$

$$\frac{-2}{x+3} = \frac{1}{x+1}$$

$$\frac{2x+1}{(x+2)(x-2)} + \frac{5(x+2)}{(x+2)(x-2)}$$

$$\frac{2x+1+5x+10}{(x+2)(x-2)}$$

$$\boxed{\frac{7x+11}{(x+2)(x-2)}}$$

⑦

Linear Functions - Assignment

1. Find the equation of the line in slope-intercept form, with the given slope, passing through the given point.

a. $m = -7, (-3, -7)$

$$\begin{aligned} y + 7 &= -7(x + 3) \\ y + 7 &= -7x - 21 \\ \boxed{y} &= -7x - 28 \end{aligned}$$

b. $m = \frac{-1}{2}, (2, -8)$

$$\begin{aligned} y + 8 &= -\frac{1}{2}(x - 2) \\ 2y + 16 &= -x + 2 \\ 2y &= -x - 14 \\ \boxed{y} &= -\frac{1}{2}x - 7 \end{aligned}$$

c. $m = \frac{2}{3}, (-6, \frac{1}{3})$

$$\begin{aligned} y - \frac{1}{3} &= \frac{2}{3}(x + 6) \\ 3y - 1 &= 2x + 12 \\ 3y &= 2x + 13 \\ \boxed{y} &= \frac{2}{3}x + \frac{13}{3} \end{aligned}$$

2. Find the equation of the line in slope-intercept form, passing through the following points.

a. $(-3, 6)$ and $(-1, 2)$

$$m = \frac{2-6}{-1+3} = \frac{-4}{2} = -2$$

$$\begin{aligned} y - 6 &= -2(x + 3) \\ y - 6 &= -2x - 6 \\ \boxed{y} &= -2x \end{aligned}$$

b. $(-7, 1)$ and $(3, -4)$

$$m = \frac{-4-1}{3+7} = \frac{-5}{10} = -\frac{1}{2}$$

$$\begin{aligned} y - 1 &= -\frac{1}{2}(x + 7) \\ 2y - 2 &= -x - 7 \\ 2y &= -x - 5 \\ \boxed{y} &= -\frac{1}{2}x - \frac{5}{2} \end{aligned}$$

c. $(-2, \frac{2}{3})$ and $(\frac{1}{2}, 1)$

$$m = \frac{1-\frac{2}{3}}{\frac{1}{2}+2} = \frac{\frac{1}{3}}{\frac{5}{2}} = \frac{2}{15}$$

$$\begin{aligned} y - 1 &= \frac{2}{15}(x - \frac{1}{2}) \\ 15y - 15 &= 2x - 1 \\ \boxed{y} &= \frac{2}{15}x + \frac{14}{15} \end{aligned}$$

3. Write equations of the line through the given point a) parallel and b) normal to the given line.

a. $(5, -3), x + y = 4$ $y = -x + 4$

$$y + 3 = -1(x - 5)$$

$$y + 3 = -x + 5$$

$$\boxed{y = -x + 2}$$

parallel

$$y + 3 = 1(x - 5)$$

$$y + 3 = x - 5$$

$$\boxed{y = x - 8}$$

perp.

b. $(-6, 2), 5x + 2y = 7$ $2y = -5x + 7$

$$y - 2 = -\frac{5}{2}(x + 6)$$

$$2y - 4 = -5x - 30$$

$$2y = -5x - 26$$

$$\boxed{y = -\frac{5}{2}x - 13}$$

parallel

c. $(-3, -4), y = -2$ $\boxed{y = -2}$

$$y + 4 = 0(x + 3)$$

$$\boxed{y = -4}$$

parallel

~~#~~ perp

4. Find an equation of the line containing $(4, -2)$ and parallel to the line containing $(-1, 4)$ and $(2, 3)$. Put your answer in general form.

$$y + 2 = -\frac{1}{3}(x - 4)$$

$$3y + 6 = -x + 4$$

$$\boxed{x + 3y = -2}$$

$$m = \frac{3-4}{2+1} = -\frac{1}{3}$$

5. Find k if the lines $3x - 5y = 9$ and $2x + ky = 11$ are a) parallel and b) perpendicular.

a) $-5y = -3x + 9$

$$y = \frac{3}{5}x - \frac{9}{5}$$

$$\frac{3}{5} = -\frac{2}{k}$$

$$3k = -10$$

$$\boxed{k = -10/3}$$

$ky = -2x + 11$

$$y = -\frac{2}{k}x + \frac{11}{k}$$

b) $\frac{3}{5} = -\frac{k}{2}$

$$5k = 6$$

$$\boxed{k = 6/5}$$

(8)